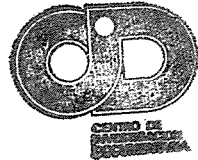


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GEAR HANDBOOK

The Design, Manufacture, and
Application of Gears



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